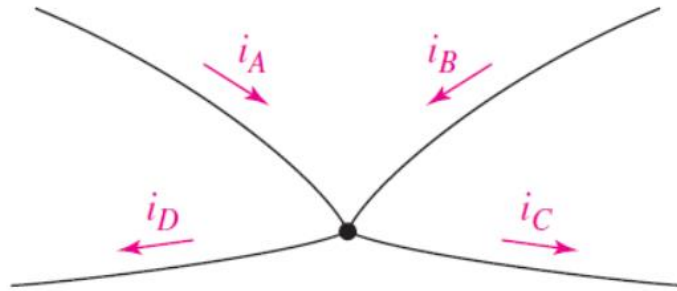

Optoelectronics Lab

KCL, KVL

Kirchhoff's Current Law

- The algebraic sum of the currents entering any node is zero.

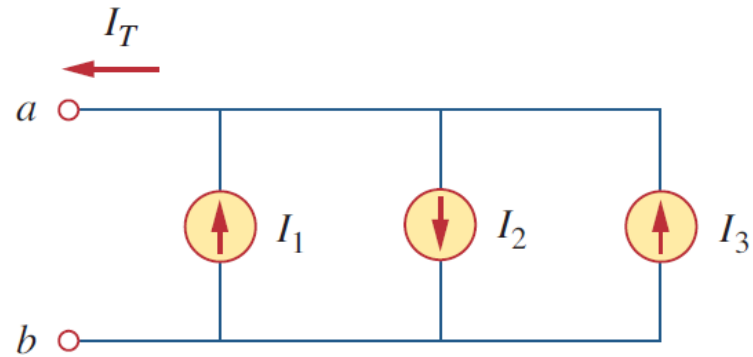


■ **FIGURE 3.2** Example node to illustrate the application of Kirchhoff's current law.

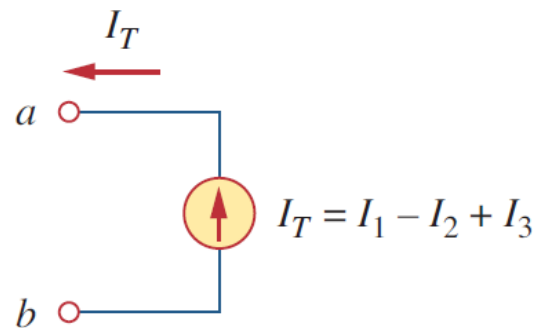
$$i_A + i_B + (-i_C) + (-i_D) = 0$$

$$(-i_A) + (-i_B) + i_C + i_D = 0$$

$$i_A + i_B = i_C + i_D$$



(a)



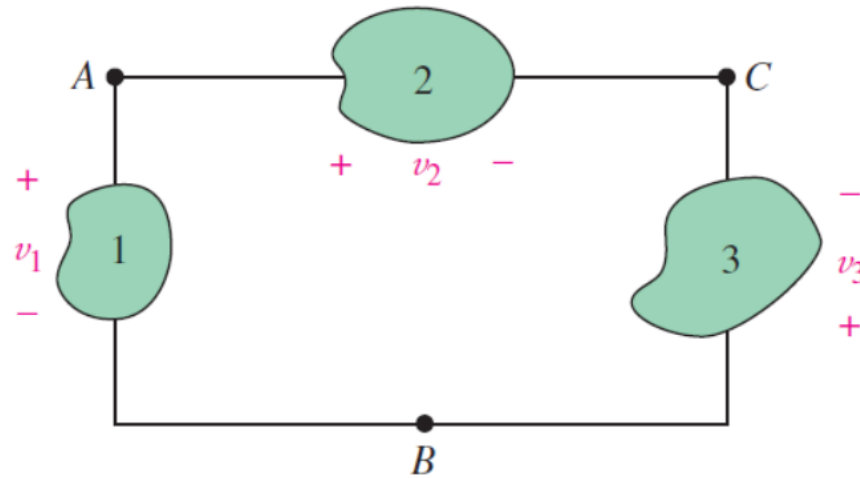
(b)

Figure 2.18

Current sources in parallel: (a) original circuit, (b) equivalent circuit.

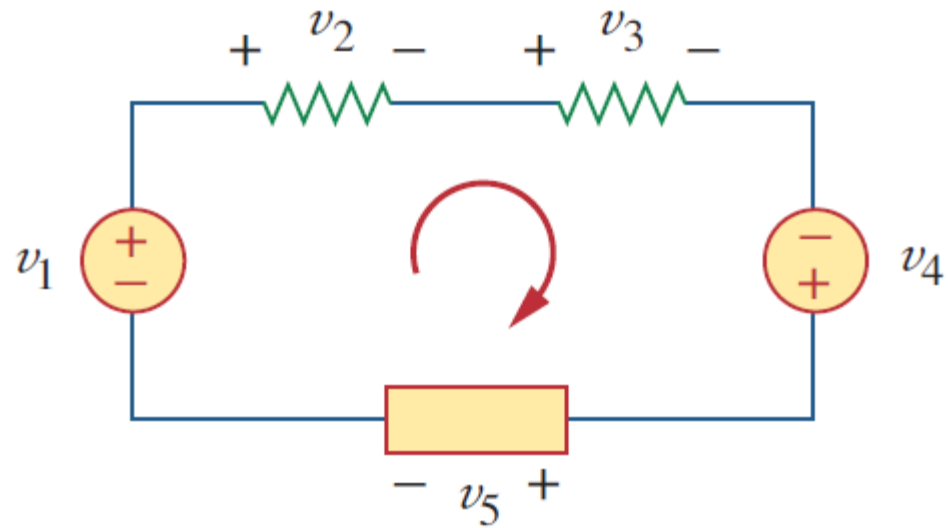
Kirchhoff's Voltage Law

- The algebraic sum of the voltages around any closed path is zero.



$$v_1 = v_2 - v_3$$

$$v_1 + v_2 + v_3 + \cdots + v_N = 0$$



$$-v_1 + v_2 + v_3 - v_4 + v_5 = 0$$

$$v_2 + v_3 + v_5 = v_1 + v_4$$

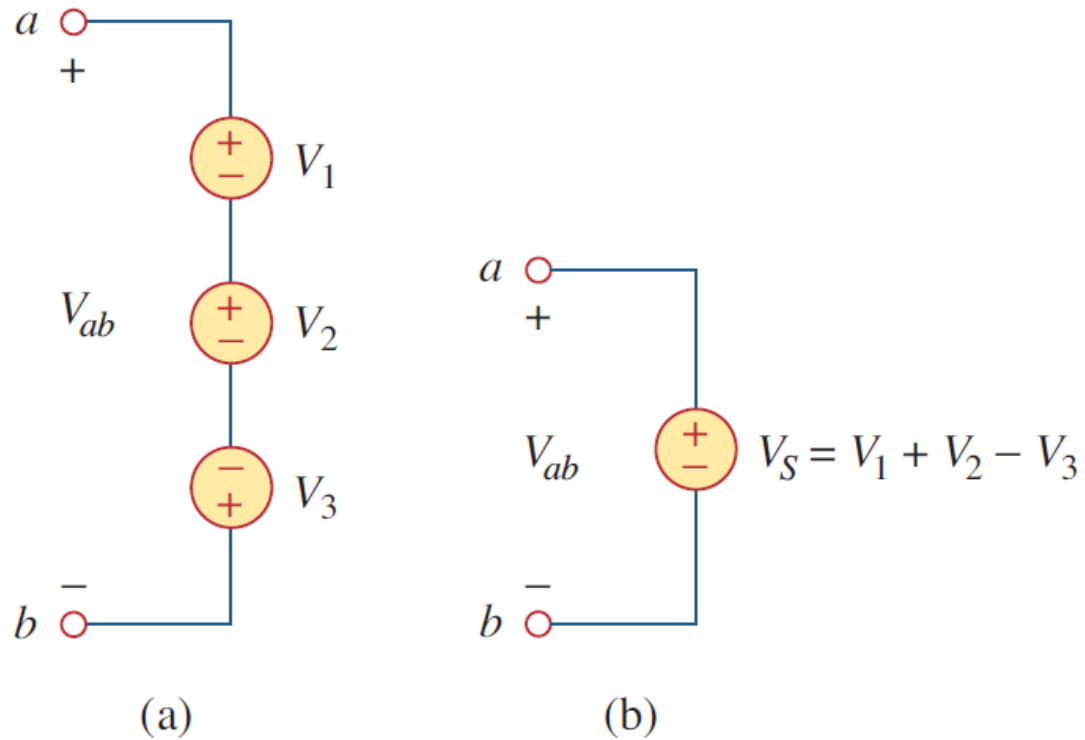
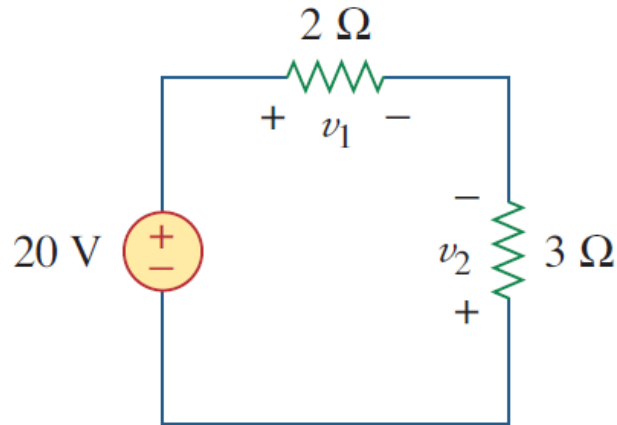


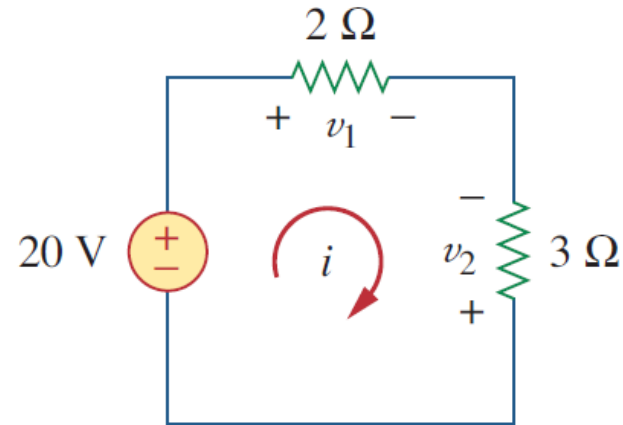
Figure 2.20

Voltage sources in series: (a) original circuit, (b) equivalent circuit.

Example



(a)



(b)

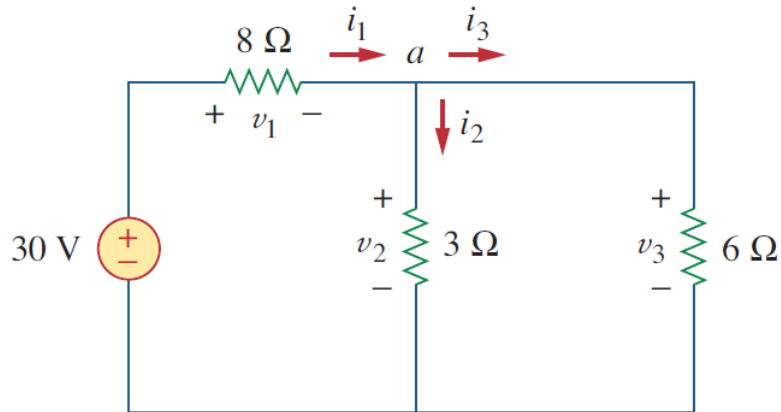
$$v_1 = 2i, \quad v_2 = -3i$$

$$-20 + v_1 - v_2 = 0$$

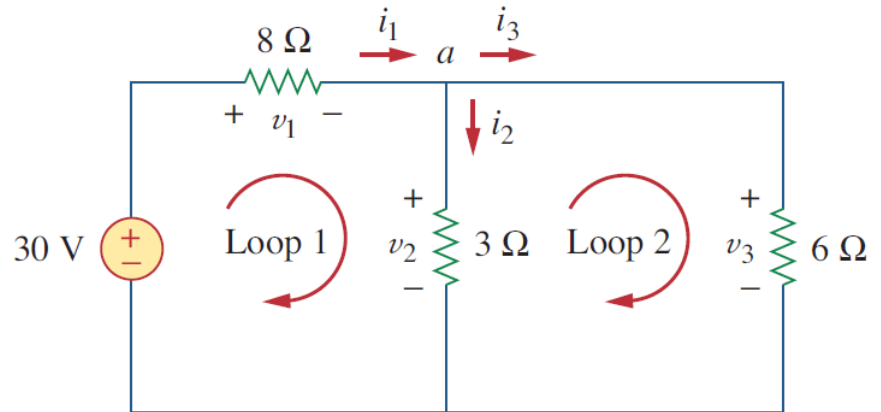
$$-20 + 2i + 3i = 0 \quad \text{or} \quad 5i = 20 \quad \Rightarrow \quad i = 4 \text{ A}$$

$$v_1 = 8 \text{ V}, \quad v_2 = -12 \text{ V}$$

Example



(a)



(b)

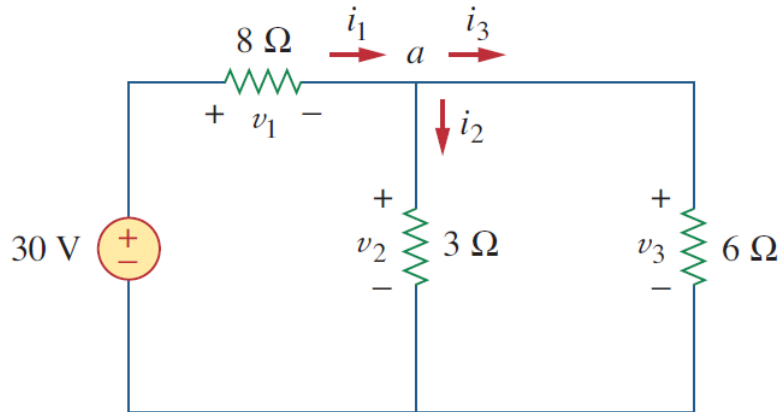
$$v_1 = 8i_1, \quad v_2 = 3i_2, \quad v_3 = 6i_3$$

$$i_1 - i_2 - i_3 = 0$$

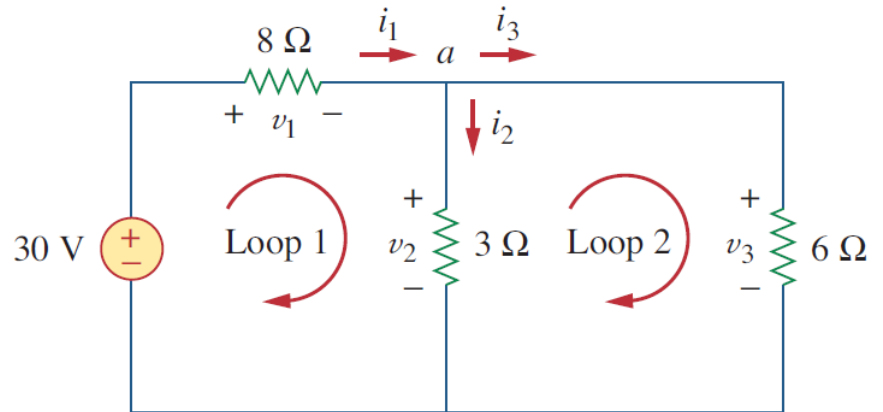
$$-30 + v_1 + v_2 = 0$$

$$-30 + 8i_1 + 3i_2 = 0$$

Example



(a)



(b)

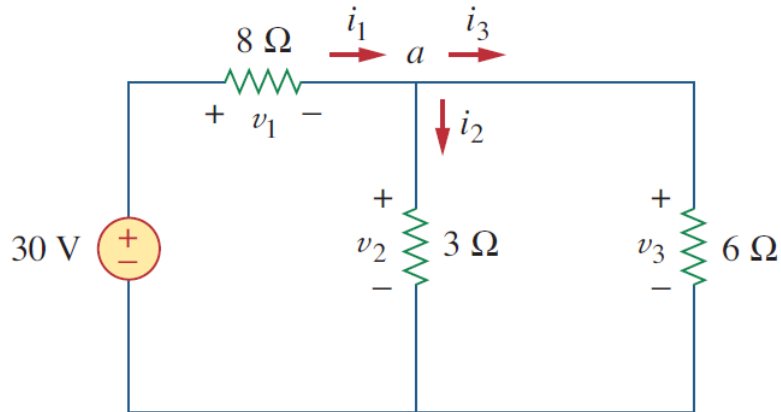
$$-v_2 + v_3 = 0 \quad \Rightarrow \quad v_3 = v_2$$

$$6i_3 = 3i_2 \quad \Rightarrow \quad i_3 = \frac{i_2}{2}$$

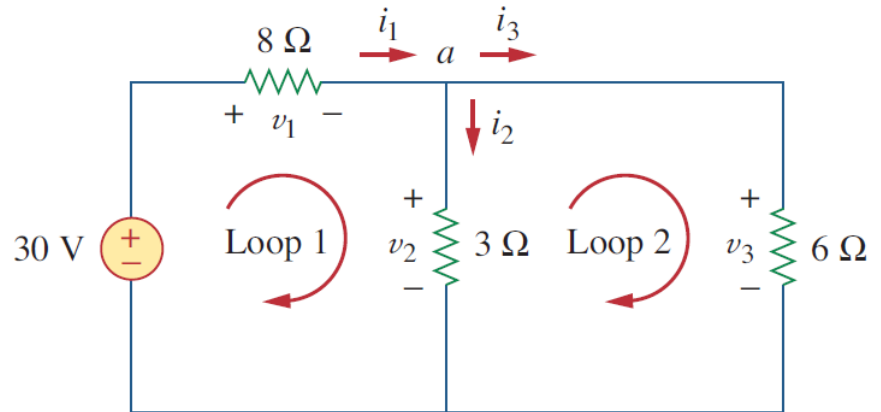
$$i_2 = 2 \text{ A} \quad i_1 = 3 \text{ A}, \quad i_3 = 1 \text{ A}$$

$$v_1 = 24 \text{ V}, \quad v_2 = 6 \text{ V}, \quad v_3 = 6 \text{ V}$$

Example



(a)



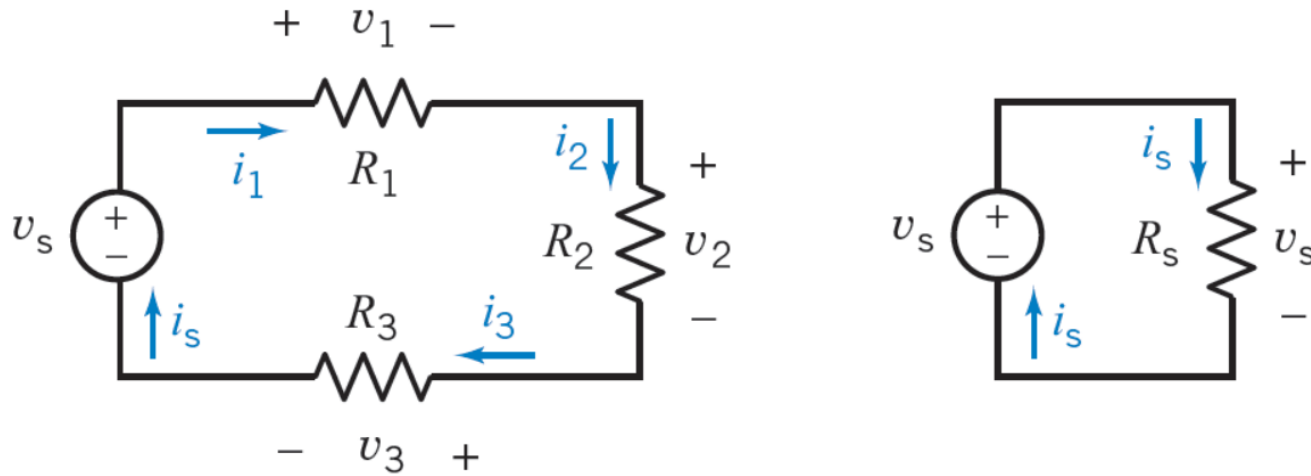
(b)

$$-30 + v_1 + v_2 = 0$$

$$-v_2 + v_3 = 0 \quad \Rightarrow \quad v_3 = v_2$$

$$\frac{v_1}{8} = \frac{v_2}{3} + \frac{v_3}{6}$$

Series Resistors



$$v_1 + v_2 + v_3 - v_s = 0$$

$$R_1 i_1 + R_2 i_2 + R_2 i_3 - v_s = 0 \Rightarrow R_1 i_1 + R_2 i_1 + R_2 i_1 = v_s$$

$$i_1 = \frac{v_s}{R_1 + R_2 + R_3}$$

$$\dot{i}_s = \frac{v_s}{R_1 + R_2 + R_3}$$

$$\dot{i}_s = \frac{v_s}{R_s}$$

$$R_s = R_1 + R_2 + R_3$$

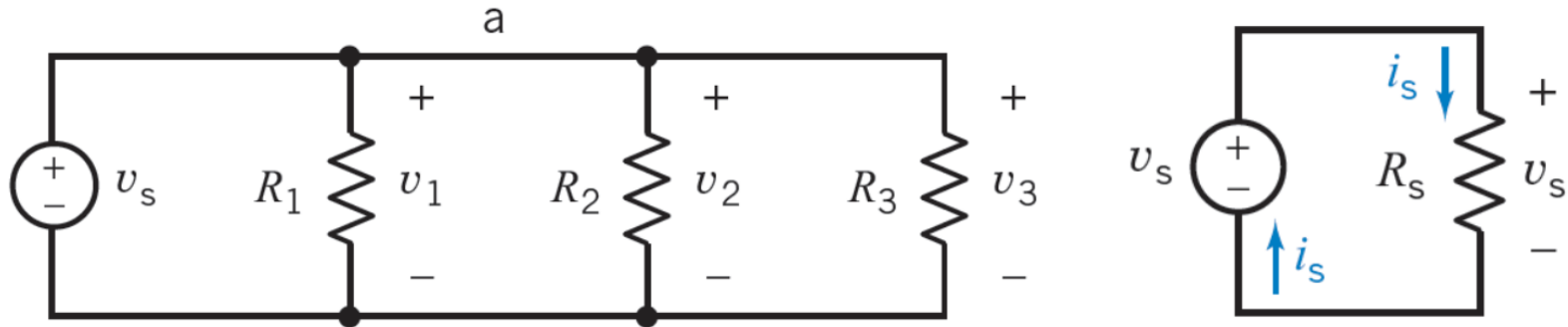
Voltage Division

$$v_1 = R_1 i_S = \frac{R_1}{R_1 + R_2 + R_3} v_S$$

$$v_2 = R_2 i_S = \frac{R_2}{R_1 + R_2 + R_3} v_S$$

$$v_3 = R_3 i_S = \frac{R_3}{R_1 + R_2 + R_3} v_S$$

Parallel Resistors



$$i_s = i_1 + i_2 + i_3 = \frac{v_s}{R_1} + \frac{v_s}{R_2} + \frac{v_s}{R_3} = \left(\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} \right) v_s$$

$$i_s = \left(\frac{1}{R_s} \right) v_s$$

$$\frac{1}{R_s} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} \Rightarrow R_s = \frac{1}{\left(\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} \right)}$$

Current Division

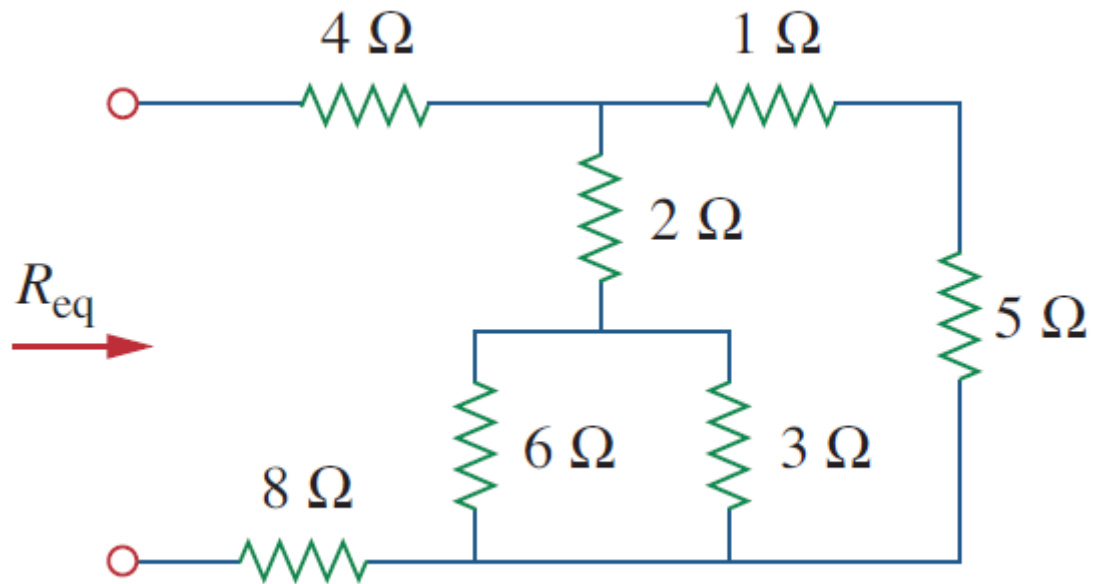
$$i_1 = \frac{v_S}{R_1} = \frac{1}{R_1} R_S i_S = \frac{\frac{1}{R_1}}{\left(\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} \right)} i_S$$

$$i_2 = \frac{v_S}{R_2} = \frac{1}{R_2} R_S i_S = \frac{\frac{1}{R_2}}{\left(\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} \right)} i_S$$

$$i_3 = \frac{v_S}{R_3} = \frac{1}{R_3} R_S i_S = \frac{\frac{1}{R_3}}{\left(\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} \right)} i_S$$

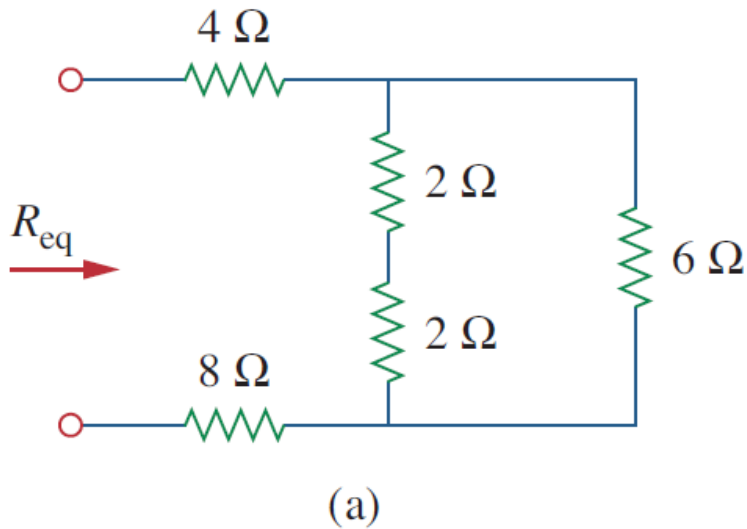
$$\frac{1}{R_S} = \frac{1}{R_1} + \frac{1}{R_2} \Rightarrow R_S = \frac{1}{\left(\frac{1}{R_1} + \frac{1}{R_2}\right)} = \frac{R_1 R_2}{R_1 + R_2}$$

Example

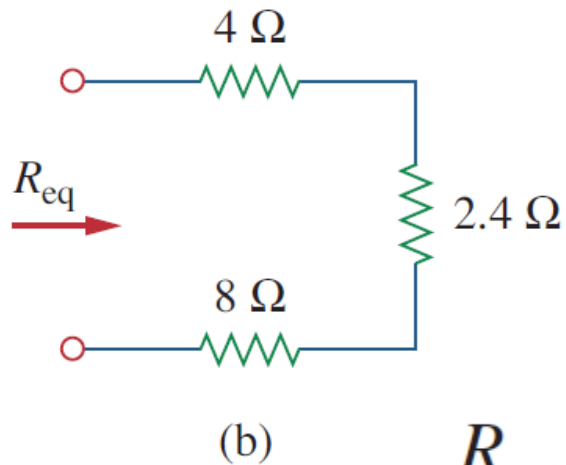


$$6\ \Omega \parallel 3\ \Omega = \frac{6 \times 3}{6 + 3} = 2\ \Omega$$

$$1\ \Omega + 5\ \Omega = 6\ \Omega$$



$$4 \Omega \parallel 6 \Omega = \frac{4 \times 6}{4 + 6} = 2.4 \Omega$$



$$R_{eq} = 4 \Omega + 2.4 \Omega + 8 \Omega = 14.4 \Omega$$

Breadboard

